

FORMULA 4.272.8

$$\int_0^1 \left(\ln \frac{1}{x}\right)^{n-1} \frac{x^{\nu-1} dx}{1+x} = (n-1)! \sum_{k=0}^{\infty} \frac{(-1)^k}{(\nu+k)^n}$$