FORMULA 3.223.2

$$\int_0^\infty \frac{x^{\mu-1}\,dx}{(x+b)(a-x)} = \frac{\pi}{(a+b)\,\sin\pi\mu}\left(b^{\mu-1} + a^{\mu-1}\cos\mu\pi\right)$$