

**NEW FORMULA 4.132.1**

The original formula is

$$\int_0^{\infty} \frac{\sin ax \sinh \beta x}{e^{\gamma x} - 1} dx = -\frac{a}{2(a^2 + \beta^2)} + \frac{\pi}{2\gamma} \frac{\sinh \frac{2\pi a}{\gamma}}{\cosh \frac{2\pi a}{\gamma} - \cos \frac{2\pi \beta}{\gamma}} + \frac{i}{2\gamma} \left[ \psi \left( \frac{\beta}{\gamma} + i \frac{a}{\gamma} + 1 \right) - \psi \left( \frac{\beta}{\gamma} - i \frac{a}{\gamma} + 1 \right) \right]$$

the change of variable  $t = \gamma x$  and replacing  $a/\gamma$  by  $a$  and  $\beta/\gamma$  by  $b$  gives the new form

$$\int_0^{\infty} \frac{\sin ax \sinh bx}{e^x - 1} dx = -\frac{a}{2(a^2 + b^2)} + \frac{\pi}{2} \frac{\sinh 2\pi a}{\cosh 2\pi a - \cos 2\pi b} + \frac{i}{2} [\psi(b + ia + 1) - \psi(b - ia + 1)]$$