

FORMULA 4.221.3

$$\int_0^1 \ln \left(\frac{1-ax}{1-a} \right) \frac{dx}{\ln x} = - \sum_{k=1}^{\infty} a^k \frac{\ln(1+k)}{k}$$