FORMULA 4.272.11

$$\int_0^1 \left(\ln \frac{1}{x} \right)^{n-1} \frac{1 - x^m}{1 - x} \, dx = (n-1)! \sum_{k=1}^{m} \frac{1}{k^n}$$