

FORMULA 4.539

$$\int_0^{\infty} x^{s-1} \tan^{-1}(ae^{-x}) dx = \frac{a\Gamma(s)}{2^{s+1}} \Phi\left(-a^2, s+1, \frac{1}{2}\right)$$