
You have all class to complete this. You may work in groups.

1. (a) [1pt] Evaluate the integral

$$\int_0^{\sqrt{\pi}} \int_y^{\sqrt{\pi}} \sin(x^2) \, dx \, dy.$$

- (b) [1pt] Set up an iterated polar integral for $\iint_R xy \, dA$, where R is the region inside the circle $r = 2 \sin \theta$ and above $y = 1$. Do not evaluate.

2. [3pts] Evaluate

$$\iint_R 3xy \, dA$$

where R is region bounded by the curves $x + 3y = 1$, $x + 3y = 3$, $x - y = 1$ and $x - y = -1$.

3. (a) [1pt] Let D the solid region inside the cone $z = \sqrt{3(x^2 + y^2)}$, outside of $x^2 + y^2 + z^2 = 4$ and below $z = 6$. Write the integral $\iiint_D zy \, dV$ as a triple iterated integral in spherical coordinates. Do not evaluate.
- (b) [1pt] Let D be the region in the first octant which is below the plane $x + 2y + 3z = 6$. Write the integral $\iiint_D xy \, dV$ as a triple iterated integral in rectangular coordinates. Do not evaluate.

4. [3pts] Find the volume of the region D bounded above by the sphere $x^2 + y^2 + z^2 = 2$ and below by the paraboloid $z = x^2 + y^2$.